# NMA-Task Documentation 

Michael Glenister

Feb 03, 2020
1 Introduction ..... 1
1.1 PyMOL Plugin ..... 1
1.2 Cite this project ..... 1
1.3 Contributing ..... 1
1.4 License ..... 2
2 Installation ..... 3
2.1 Platform compatibility ..... 3
2.2 Download the project ..... 3
2.3 Installing dependencies ..... 3
3 Normal Mode Analysis (NMA) ..... 5
4 Principal Component Analysis (PCA) ..... 9
5 Kernel PCA (kPCA) ..... 11
6 Incremental PCA ..... 13
7 Multi-dimensional scaling (MDS) ..... 15
8 t-Distributed Stochastic Neighbor Embedding (t-SNE) ..... 17
9 NMA Scripts ..... 19
9.1 Coarse grain ..... 19
9.2 ANM ..... 20
9.3 Mean square fluctuation ..... 20
9.4 Assembly Covariance ..... 21
9.5 Conformation mode ..... 24
9.6 Combination mode ..... 24
9.7 Mode visualisation ..... 25
10 PCA Scripts ..... 29
10.1 PCA on Cartesian coordinates ..... 30
10.2 PCA on internal coordinates ..... 31
10.3 MDS (Multi-dimensional scaling) on MD trajectory ..... 32
10.4 t-SNE on MD trajectory ..... 33
11 NMA Tutorial ..... 35
11.1 Aim ..... 35
11.2 Create a working directory ..... 35
11.3 Preparation of structure of the mature capsid ..... 35
11.4 Preparation of the structure of the A-particle capsid ..... 36
11.5 Coarse grain ..... 36
11.6 Mode decomposition ..... 37
11.7 Identification of modes that contribute to the conformational change ..... 38
11.8 Conformation mode ..... 39
11.9 Combination mode ..... 41
11.10 Mode visualisation ..... 42
11.11 Mean square fluctuation (MSF) ..... 48
11.12 Assembly Covariance ..... 49
12 PCA Tutorial ..... 55
12.1 PCA of a MD trajectory ..... 55
12.2 MDS (Multi-dimensional scaling) on a MD trajectory ..... 60
12.3 t -SNE on a MD trajectory ..... 60
13 pyMODE-TASK- PyMOL plugin ..... 65

## CHAPTER 1

## Introduction

MODE-TASK is a collection of tools for analysing normal modes and performing principal component analysis on biological assemblies.

Novel coarse graining techniques allow for analysis of very large assemblies without the need for high performance computing clusters and workstations.

### 1.1 PyMOL Plugin

A PyMOL plugin for MODE-TASK has been made available here.

### 1.2 Cite this project

Caroline Ross, Bilal Nizami, Michael Glenister, Olivier Sheik Amamuddy, Ali Rana Atilgan, Canan Atilgan, Özlem Tastan Bishop; MODE-TASK: Large-scale protein motion tools, Bioinformatics, May 2018 , https://doi.org/10.1093/ bioinformatics/bty427

### 1.3 Contributing

To contribute to the documentation please follow this guide.
To contribute to the source code, submit a pull request to our Github repository.
Please follow the PEP8 style guide for python tools. A number of tools are available to help with checking PEP8 compliance including flake 8

Don't reformat code that is unrelated to you work unless the pull request or commit is specifically to format for PEP8 compliance.

### 1.4 License

The project is licensed under GNU GPL 3.0

## CHAPTER 2

## Installation

### 2.1 Platform compatibility

A Linux-like operating system is recommended. However, MODE-TASK is compatible with most platforms which are able to run Python 2.7 or Python 3.6.

A compiler is required to compile $\mathrm{C}++$ from source, in this instance we use $\mathrm{g}++$.

### 2.2 Download the project

MODE-TASK can be cloned from its GitHub repository

```
git clone https://github.com/RUBi-ZA/MODE-TASK.git
cd MODE-TASK
```


### 2.3 Installing dependencies

## Ubuntu:

Python 2.7 with pip and virtualenv

```
sudo apt-get update
sudo apt-get install python-pip virtualenv virtualenvwrapper
virtualenv venv
source venv/bin/activate
pip install -r requirements.txt
```

Python 3.6 with pip and virtualenv

```
sudo apt-get update
sudo apt-get install python3-pip virtualenv virtualenvwrapper
virtualenv venv
source venv/bin/activate
pip3 install -r requirements.txt
```

Conda

```
conda create -n mode_task
source activate mode_task
conda install -c conda-forge numpy
conda install -c conda-forge cython
conda install -c omnia mdtraj
conda install -c conda-forge scipy
conda install -c conda-forge pandas
conda install -c conda-forge sklearn-contrib-lightning
conda install -c conda-forge matplotlib
```

To install conda follow their documentation
OSX:

```
brew update
brew install python gcc
pip install virtualenv virtualenvwrapper
```


## Windows:

Enable Windows Subsystem for Linux (WSL) by following these instructions.
Install the system dependencies as with Ubuntu above.

## Chapter 3

## Normal Mode Analysis (NMA)

NMA analyses the oscillations of a structure. For proteins, it is useful for studying the large amplitude motions for a selected conformation. The main assumption is that the motions are harmonic. Thus, each normal mode, which is a concerted motion of many atoms, acts as a simple harmonic oscillator, and it is independent of all the other normal modes.

For a harmonic oscillator with a mass $m$ supported on a spring with force constant $k$, the potential energy of the system, $V=k x^{2}$, for an extension $x$ leads to the restoring force,

$$
\mathbf{F}=-\frac{d V}{d x}=-k x
$$

By substituting this Hooke's Law force into Newton's Law, $\mathbf{F}=m$ a leads to the differential equation,

$$
-k x=m \frac{d^{2} x}{d t^{2}}
$$

The solution is,

$$
-k x=-4 \pi^{2} v^{2} m x
$$

with $v$ being the frequency of the vibration.
In three dimensions and for a set of $N$ atoms, one has the corresponding generalized equation,

$$
-\mathbf{H X}=-4 \pi^{2} v^{2} \mathbf{X}
$$

where $\mathbf{H}$ is the $3 N \mathrm{x} 3 N$ Hessian symmetric matrix of force constants and $\mathbf{X}$ is the $3 N \mathrm{x} 1$ vector of the positions of the atoms. The solutions of the equation may be cast in the form of an eigenvalue decomposition of $\mathbf{H}$ where the eigenvectors are the mass weighted displacements of the normal coordinates; i.e. the independent vibrational motions of the collection of atoms. The corresponding eigenvalues are the negative of the squared normal mode frequencies of each mode. $\mathbf{H}$ has exactly six zero eigenvalues for the translations and rotations of the molecule in three dimensional space.

In NMA of proteins, it is central to obtain a good representation of the protein for a proper analysis of the available modes of motion. One approach would be to obtain the Hessian matrix from the second derivatives of the energy for the conformation of interest following a very stringent minimization of the molecule. The latter is important as NMA
is based on the harmonic assumption which is only a valid approximation at the bottom of the potential energy minima. For the complex potentials representing interactions in proteins in the water environment, these second derivatives may be obtained through numerical methods which are extremely costly.
Alternatively, $\mathbf{H}$ may be approximated by the variance-covariance matrix of the protein, obtained from a molecular dynamics (MD) simulation of suitable length. This is relevant as it may be shown through employing statistical mechanics that the average displacements of nodes from a mean structure for an atom $i, \Delta \mathbf{R}_{i}$ are related to those of all other atoms through the relationship,

$$
<\Delta \mathbf{R}_{i} \cdot \Delta \mathbf{R}_{j}>=3 k_{B} T \mathbf{H}^{-1}
$$

It is important to select the length of the MD simulation for this procedure such that the molecule samples only the state of interest, ${ }^{1}$ since when more than a single potential energy well along the conformational space of the molecule is sampled, the harmonic assumption would again fail.

As a third alternative for obtaining the Hessian, one may make use of the elastic network property of a folded protein. Here, the assumption is that, once a protein folds to a functionally relevant conformation, its total energy is represented by a simple harmonic potential such that residues are connected to their nearest neighbors via elastic springs. By further employing the assumption that the spring constants, $\gamma$, are equivalent in all pairs of interactions, one arrives at the anisotropic network model (ANM). ${ }^{2}$
$\mathbf{H}$ is thus composed of $N \mathrm{x} N$ super-elements, i.e.,

$$
\mathbf{H}=\left[\begin{array}{cccc}
\mathbf{H}_{1,1} & \mathbf{H}_{1,2} & \cdots & \mathbf{H}_{1, \mathbf{N}} \\
\mathbf{H}_{2,1} & & & \mathbf{H}_{2, \mathbf{N}} \\
\vdots & & & \vdots \\
\mathbf{H}_{\mathbf{N}, 1} & & & \mathbf{H}_{\mathbf{N}, \mathbf{N}}
\end{array}\right]
$$

where each super-element $\mathbf{H}_{\mathbf{i j}}$ is a $3 \times 3$ matrix that holds the anisotropic information regarding the orientation of nodes $i, j$ :

$$
\mathbf{H}_{\mathbf{i j}}=\left[\begin{array}{lll}
\partial^{2} V / \partial X_{i} \partial X_{j} & \partial^{2} V / \partial X_{i} \partial Y_{j} & \partial^{2} V / \partial X_{i} \partial Z_{j} \\
\partial^{2} V / \partial Y_{i} \partial X_{j} & \partial^{2} V / \partial Y_{i} \partial Y_{j} & \partial^{2} V / \partial Y_{i} \partial Z_{j} \\
\partial^{2} V / \partial Z_{i} \partial X_{j} & \partial^{2} V / \partial Z_{i} \partial Y_{j} & \partial^{2} V / \partial Z_{i} \partial Z_{j}
\end{array}\right]
$$

Denoting the separation between nodes $i$ and $j$ by $S_{i j}$, the elements of the off-diagonal super-elements $\mathbf{H}_{\mathbf{i j}}$ are given by:

$$
\partial^{2} V / \partial X_{i} \partial Y_{j}=-\gamma\left(X_{j}-X_{i}\right)\left(Y_{j}-Y_{i}\right) / S_{i j}^{2}
$$

and those of the diagonal super-elements $\mathbf{H}_{\mathbf{i j}}$ are obtained via,

$$
\begin{gathered}
\partial^{2} V / \partial X_{i}^{2}=\gamma \sum_{j}\left(X_{j}-X_{i}\right)^{2} / S_{i j}^{2} \quad \text { for the diagonal terms } \\
\partial^{2} V / \partial X_{i} \partial Y_{j}=\gamma \sum_{j}\left(X_{j}-X_{i}\right)\left(Y_{j}-Y_{i}\right) / S_{i j}^{2} \quad \text { for the off-diagonal terms. }
\end{gathered}
$$

In this representation of the protein, the structure is coarse-grained at the level of a residue, usually through the coordinates of $\mathbf{C}_{\alpha}$ or $\mathbf{C}_{\beta}$ atoms obtained from the protein data bank. Moreover, pairs of nodes are assumed to interact if they are within a pre-selected cut-off distance, $r_{c}$. For large structures such as viruses, further coarse graining may be shown to well describe the most collective modes of motion.

The selection of $r_{c}$ has been the cause of much research. While it is clear that there is a lower bound where the condition of six zero eigenvalues of $\mathbf{H}$ should be satisfied, distances in the range 10-25 $\AA$ have been employed in the

[^0]literature. It has been shown by a systematic study of increasing $r_{c}$ that the collective modes of motion do not change beyond a certain value for proteins; i.e. selection of too large $r_{c}$ is safer than a too small value. ${ }^{3}$ The reason for this has been explained by expressing $\mathbf{H}$ as the sum of an essential and a trivial part. The essential part of $\mathbf{H}$ includes all the local information necessary for the correct representation of the modes. On the other hand, due to the symmetries in a protein originating from the orientational order of closely packed spheres, the effects from the long range neighbors cancel out.

## References

[^1]
## CHAPTER 4

## Principal Component Analysis (PCA)

A molecular dynamics (MD) simulation of a protein provides the positional movements of each atom with respect to a fixed reference frame at a given time. The mean squared positional fluctuations (variances) of each atom are readily calculated once the total simulation and sampling times are set. Sufficiency of both total observation period and the sampling rate are crucial in collecting the data so as to identify biologically relevant motions. Let us monitor the variance of each residue's $\mathbf{C}_{\alpha}$ or $\mathbf{C}_{\beta}$ atom during a MD simulation of a protein. Suppose that these variances do not change significantly in time, like a stationary process. This suggests that within the period of observation we have recorded the motion about one (native) conformation. Though constant in time for a given residue, the variances do change from one residue to another. It is important to distinguish the differences between the variances of different parts of the protein and to explain the root cause of these differences; e.g. while loop or disordered regions exhibit high values, relatively rigid parts, such as helices or sheets display lower variances.
$\mathrm{PCA}^{4}$ operates on the variance-covariance matrix, $\mathbf{C}$, of the protein, obtained from a MD simulation of any length; thus, the observed process need not be stationary. It is useful in distinguishing the different parts of the energy landscape sampled during the MD simulation. To obtain $\mathbf{C}$, first the protein coordinates are superimposed on a reference structure, usually the initial coordinates, or the average coordinates. The displacement vector for each residue (described by the $\mathbf{C}_{\alpha}$ or $\mathbf{C}_{\beta}$ coordinates of the residue $i$ ) at a time point $t, \Delta \mathbf{R}_{i}(t)$ is obtained. For a set of $M$ recorded coordinates, these are organized in the trajectory fluctuation matrix of order $3 N \times M$ :

$$
\Delta \mathbf{R}=\left[\begin{array}{cccc}
\Delta \mathbf{R}_{1}\left(t_{1}\right) & \Delta \mathbf{R}_{1}\left(t_{2}\right) & \cdot & \Delta \mathbf{R}_{1}\left(t_{M}\right) \\
\Delta \mathbf{R}_{2}\left(t_{1}\right) & \Delta \mathbf{R}_{2}\left(t_{2}\right) & \cdot & \Delta \mathbf{R}_{2}\left(t_{M}\right) \\
\Delta \mathbf{R}_{3}\left(t_{1}\right) & \Delta \mathbf{R}_{3}\left(t_{2}\right) & \cdot & \Delta \mathbf{R}_{3}\left(t_{M}\right) \\
\cdot & \cdot & \cdot & \cdot \\
\cdot & \cdot & \cdot & \cdot \\
\Delta \mathbf{R}_{n}\left(t_{1}\right) & \Delta \mathbf{R}_{n}\left(t_{2}\right) & & \Delta \mathbf{R}_{n}\left(t_{M}\right)
\end{array}\right]
$$

The $3 N \mathrm{x} 3 N \mathrm{C}$ matrix is then obtained via the operation,

$$
\mathbf{C}=\Delta \mathbf{R} \Delta \mathbf{R}^{\mathbf{T}}
$$

If a single energy well along the potential energy surface of a protein is sampled, then $\mathbf{C}$ approximates the inverse Hessian, $\mathbf{H}^{-1}$, as the harmonic approximation applies in this case (see NMA for details). However, if different parts

[^2]of the landscape are sampled, the decomposition of $\mathbf{C}$ will carry information on all the regions entered during the simulation. Thus, the diagonalization,
$$
\mathbf{C}=\mathbf{U} \boldsymbol{\Lambda} \mathbf{U}^{\mathbf{T}}
$$
yields the eigenvectors and the corresponding eigenvalues of the $\mathbf{C}$ matrix. $\boldsymbol{\Lambda}$ is the $3 N \mathrm{x} 3 N$ diagonal matrix holding the eigenvalues $\lambda_{i}$ with six zero values corresponding to the translations and rotations of the molecule. The $i^{\text {th }}$ row of the $\mathbf{U}$ matrix holding the eigenvector corresponding to the $i^{\text {th }}$ eigenvalue. The trajectory $\Delta \mathbf{R}$ may be projected onto the eigenvectors to obtain the principal components, $q_{i}$, which are the rows of the $3 N \times M \mathbf{Q}$ matrix.
$$
\mathbf{Q}=\mathbf{U} \Delta \mathbf{R}
$$

Since a few principal components usually carry the largest amount of information of the trajectory, the different regions of the conformational space will manifest as more than one blob in a plot of $q_{i}$ versus $q_{j}$ where $i$ and $j$ are small. Furthermore, the size of the blobs in the plots will provide information on the width of the potential wells sampled. Finally, the time points when passage between different wells occur may be pinpointed by this method. The different implementations of the construction of the C matrix and the various ways of decomposing it have been discussed in detail in the literature, ${ }^{5}$ and implemented in MODE-TASK.

## References

[^3]
## CHAPTER 5

## Kernel PCA (kPCA)

Standard PCA assumes that input data are linearly related. In cases where variables are not intrinsically linearly related the user has option to perform nonlinear generalization of PCA such as Kernel PCA. It is an extention of normal PCA, where different kernel fucntions (such as linear, RBF, polynomial, and cosine) are used to perform non-linear dimensional reduction.
$N$ points are linearly non-separable in dimension $(d<N)$. But there can be a hyperplane dividing them in a higher dimension given $N$ points, $(X i)$ it can be maped to an N -dimensional space with

$$
\Phi(\mathbf{X i}) \text { where } \Phi: \mathbf{R}^{\mathbf{d}}->\mathbf{R}^{\mathbf{n}}
$$

$\Phi$ is an arbitrary choosen fucntion.
MODE-TASK includes the tools to perform the Kernel PCA on MD trajectory, and offers the user different choices for the kernel. In Kernel PCA the input trajectory is first raised to a higher dimension by a kernel function and then PCA is performed on the elevated data. One should use Kernel PCA with caution as it is difficult to interpret the results since the input trajectory is mapped to a different feature space than conformational space. Nevertheless, Kernel PCA could be an invaluable tool in studying structural mechanisms behind protein dynamics in cases where conventional PCA is not helpful.

## chapter 6

## Incremental PCA

A major bottleneck in the speed of PCA calculation is the availability of computer memory during the loading of a MD trajectory. IPCA is a memory efficient variant of PCA, where only most substantial singular vectors are used to project the input data to a lower dimension. The IPCA algorithm uses a batch data loading approach and the incremental storage of various variables, thus achieving higher memory efficiency. MODE-TASK has implemented IPCA on MD trajectory, available through scikit-learn Python library on the original algorithm ${ }^{67}$.

## References

[^4]
## Chapter 7

## Multi-dimensional scaling (MDS)

MDS is a technique of dimensionality reduction, where measure of dissimilarity in a dataset is used. It places each input point in $N$-dimensional space while trying to preserve the original distance matrix as much as possible. MODETASK implements metric and nonmetric types of MDS for MD trajectory by using the scikit-learn library ${ }^{6}$. The Euclidean distance between internal coordinates and pairwise RMSD between the MD frames is used as dissimilarity measures in MODE-TASK.

## CHAPTER 8

## t-Distributed Stochastic Neighbor Embedding (t-SNE)

t -SNE is another dimensionality reduction method for data of high dimensions ${ }^{8} . \mathrm{t}$-SNE has been implemented for protein MD trajectories in MODE-TASK. Like MDS, the Euclidean distance between internal coordinates of a protein structure and pairwise RMSD between a set of atoms are used as measures of dissimilarity.

## References

[^5]
## CHAPTER 9

## NMA Scripts

### 9.1 Coarse grain

Takes a protein structure or biological assembly and coarse grains to select a set amount of CB atoms Command:

```
coarseGrain.py <options> --pdbFile <pdb file> --atomType <string>
```

Inputs:

| Input (*required) | Input type | Flag | Description |
| :--- | :--- | :--- | :--- |
| PDB file * | File | -- pdb | PDB structure to coarse <br> grain. Can also accept bi- <br> ological assembly (.pdb1) |
| Atom type* | String | -- atomType | Specify the type of atom <br> to be selected in CG mod- <br> els. Only CA or CB ac- <br> cepted. |
| Coarse grain level | Comma Separted String | -- cg | Level/Levels by which <br> to coarse grain protein. <br> Lower is less coarse <br> grained <br> E.g -cg 4 OR <br> E.g -cg 1,3,5 Default: 4 |
| Starting atom | Integer | -- startingAtom | Residue number of the <br> starting atom. Default: 1 |
| Output file | File | Specify a name for the <br> PDB output file. Default: <br> ComplexCG.pdb |  |

## Outputs:

| Output | Description |
| :--- | :--- |
| PDB file/s | Coarse grained protein/s or macromolecule/s |

### 9.2 ANM

Constructs an elastic network model of a protein complex and solves for the eigenvalues and eigenvectors of the system.

## Compile:

```
g++ -I cpp/src/ ANM.cpp -o ANM
```

Command:

```
ANM <options> --pdb <pdb file> --atomType <atom type>
```


## Inputs:

| Input ( <br> quired | Input <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| PDB file ${ }^{*}$ | File | -- pdb | PDB input file |
| Atom type ${ }^{*}$ | String | -- atomType | Specify the type of atom to be selected in CG models. Only CA or <br> CB accepted. |
| Cutoff | Integer | -- cutoff | Cuttoff radius in A. Default: 15 |

## Outputs:

| Output | Description |
| :--- | :--- |
| W matrix | Text file of $3 N$ eigenvalues |
| VT matrix | Text file of $3 N \mathrm{x} 3 N$ eigenvectors. Printed in rows |
| U matrix | Text file of $3 N \mathrm{x} 3 N$ eigenvectors. Printed in columns |

### 9.3 Mean square fluctuation

Calculates and returns the diagonals of the correlation matrix for a given set of modes.
The user can also compare the msf between two protein complexes. Let's say that the user has performed NMA on two coarse grained models of the same protein, and now wants to compare if the additional coarse graining decreased the accuracy. If we obtain the same mean square fluctuations for each residue, then in each model we can say that the results are comparable regardless of the coarse graining level. Obviously, we must compare only the residues that are common in each model. Hence, we specify common residues.

## Command:

```
meanSquareFluctuations.py <options> --pdb <PDB file> --wMatrix <text file> --vtMatrix
<<text file> --atomType <string>
```


## Inputs:

| Input (*required) | Input type | Flag | Description |
| :---: | :---: | :---: | :---: |
| PDB file * | File | --pdb | PDB input file |
| W matrix file * | File | --wMatrix | W values from ANM script for PDB |
| VT matrix file * | File | --vtMatrix | VT values from ANM script for Comparison PDB |
| Atom type * | String | --atomType | Specify the type of atom to be selected in CG models. Only CA or CB accepted. |
| Comparison PDB | File | --pdbC | When assigned, calculates mean square fluctuations based on common residues between the two systems. |
| W matrix file for pdbC | File | --wMatrixC | When assigned, calculates W values from ANM for Comparison PDB |
| VT matrix file for pdbC | File | --vtMatrixC | When assigned, calculates VT values from ANM for Comparison PDB |
| Selected modes | String <br> OR <br> Colon Separated String OR <br> Comma Separated String | --modes | MSFs will be calculated over specified modes. Options: 1) Single mode E.g -modes 7; 2) A range E.g -modes 7:20; 3) A list E.g -modes 8,9,11 <br> If unspecified MSFs will be calculated for the first twenty slowest modes (7:27) |

## Outputs:

| Output | Description |
| :--- | :--- |
| The following are generated for the PDB and Comparison PDB (if pdbC was assigned) |  |
| MSF text file | MSF for all residues, calculated over all modes |
| MSF modes text file | MSF for all residues, calculated for a specific mode range |
| Common residue MSF text file | MSF for all common residues, calculated over all modes |
| Common residue MSF modes text file | MSF for all common residues, calculated over a specific mode range |

### 9.4 Assembly Covariance

## Calculates and plots Covariance matrices

The user can compare the Covariance between different regions in the biological assembly, or can calculate the Covariance across the full assembly complex. The user also has the option to perform the calculation over a specified list of modes or a mode range. The function also has a zoom option that allows the user to create a Covariance plot for a particular chain within a particular asymmetric unit.

## Command:

```
assemblyCovariance.py <options> --pdb <PDB file> --wMatrix <text file> --vtMatrix
\hookrightarrow<text file> --atomType <string>
```

Inputs:

| Input ( ${ }^{*}$ required) | Input type | Flag | Description |
| :---: | :---: | :---: | :---: |
| PDB file * | File | --pdb | PDB input file |
| W matrix file * | File | --wMatrix | W values from ANM script for PDB |
| VT matrix file * | File | --vtMatrix | VT values from ANM script for Comparison PDB |
| Atom type * | String | --atomType | Specify the type of atom to be selected in CG models. Only CA or CB accepted. |
| Selected modes | String OR <br> Colon Separated String OR <br> Comma Separated String | --modes | Covariance will be calculated over specified modes Options: 1) All modes E.g -modes all; 2) Single mode E.g -modes 7; 3) A range E.g -modes 7:20; 4) A list E.g -modes 8,9,11 If unspecified, Covariance will be calculated for all modes. |
| Asymmetric Units | String OR <br> Comma Separated String | --aUnits | Covariance will be calculated and plotted for specified asymmetric units <br> Options: 1) Single unit <br> E.g -aUnits <br> 5; <br> 2) A list of units E.g -aUnits 1,3 <br> If unspecified, Covariance will be calculated for the first asymmetric unit in the assembly. |
| Zoom | Comma Separated String | --zoom | If specified, Covariance will be calculated and plotted for a specified chain in a specified unit. Only format accepts is: [Unit,Chain] <br> (Chain specifier must match chain label in PDB file) The above calculates the co- |
| 9.4. Assembly Cold |  |  | variance for th23 second chain in the first asymmetric unit. |

## Outputs:

| Output | Description |
| :--- | :--- |
| Covariance Plots | Covariance Matrices plotted as a Linear Segmented Color map |
| Matrix text files | Covariance Matrices printed in .txt format |

### 9.5 Conformation mode

Identifies modes responsible for the conformational change of a molecule.

## Command:

```
conformationMode.py <options> --pdbConf <PDB file> --pdbANM <PDB file> --vtMatrix
\hookrightarrow<text file> --atomType <string>
```


## Inputs:

| Input ( <br> quire- $)$ | Input <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| Unaligned PDB <br> file * | File | -- pdbConf | PDB file of the conformational change |
| PDB $*$ | File | -- pdbANM | PDB file that was used to run ANM |
| VT matrix file * | File | -- vtMatrix Eigenvetors obtained from ANM script |  |
| Atom type * | String | -- atomType | Specify the type of atom to be selected in CG models. Only CA or <br> CB accepted. |
| Output file | File | -- output | Specify a name for the output file. Default: ModesOfCon- <br> fChange.txt |

## Outputs:

| Output | Description |
| :--- | :--- |
| Conformation file | Text file with the overlap and correlation of each mode |

### 9.6 Combination mode

Calculates the combined overlap and correlation for specified set of modes to a known conformational change. This script also calculates the overlap and correlation per chain in each asymmetric unit for the specified modes. This allows the user to determine which parts of the complex, in each mode, contribute the most to the overall conformational change.

## Command:

```
combinationMode.py <options> --pdbConf <PDB file> --pdbANM <PDB file> --vtMatrix
\hookrightarrow<text file> --modes <comma separated string> --atomType <string>
```


## Inputs:

| Input ( <br> quired re- | Input <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| Unaligned <br> PDB file * | File | -- pdbCon | PDB file of the conformational change |
| PDB * | File | -- pdbANM | PDB file that was used to run ANM |
| VT matrix file <br> $*$ | File | -- vtMatr | iEigenvetors obtained from ANM script |
| Modes * | Integer | -- modes | Calculate the overlap for a combination of specific modes. Numbers are <br> separated by commas: 1,5,7 |
| Atom type * | String | -- atomTyppecify the type of atom to be selected in CG models. Only CA or CB |  |
| accepted. |  |  |  |

## Outputs:

| Output | Description |
| :--- | :--- |
| Combination <br> file | Text file with the overlap and correlation of each mode as well as the combined overlap and <br> correlation for the modes specified |
| Break down <br> per unit file | Text file with the overlap and correlation calculated for each chain in each asymmetric unit in the <br> complex. Calculations are performed for each specified mode. |

### 9.7 Mode visualisation

Generates a set of frames, where eigenvectors are plotted as a set of unit vectors multiplied by an increasing factor in each frame. Vectors are also plotted as arrows that can be viewed in the tool VMD

## Command:

```
visualiseVector.py <options> --pdb <PDB file> --vtMatrix <text file> --mode <int> --
\hookrightarrowatomType <string> --direction <int>
```


## Inputs:

| Input ( *required) | Input type | Flag | Description |
| :---: | :---: | :---: | :---: |
| Coarse grained PDB file * | File | --pdb | Coarse grained PDB input file |
| Mode index value * | Ingeter | --mode | Value specifying the index of the mode |
| VT matrix file * | File | --vtMatrix | VT values from ANM script |
| Atom type * | String | --atomType | Specify the type of atom to be selected in CG models. Only CA or CB accepted. |
| Direction | Boolean integer (1 or -1) | --direction | Direction of overlap correction. Default $=1$ |
| Arrow head | float | --head | Radius of cone that forms the head of each vector arrow |
| Arrow tail | float | --tail | Radius of cylinder that forms the tail of each vector arrow |
| Arrow length | float | --arrowLength | Specify a factor by which to increase or decrease the length of each arrow E.g <br> -arrowLength <br> 2 doubles the default length and -arrowLength 0.5 halves the default length |
| Colours | Comma Separted String | --colourByChain | Colour the vectors arrows of each chain. E.g for a two chain protein <br> -colourByChain <br> blue,red <br> will colour the arrows of Chain A as blue and Chain B as red |
| Asymmetric Units | String <br> OR <br> Comma Separated String | --aUnits | Vector frames and arrows will be plotted for specified asymmetric units Options: 1) Single unit E.g -aUnits 5 <br> 2) A list of units E.g -aUnits 1,3 |
| Chain | String | --chain | Draws arrows only for the specified chain. This option only accepts a single chain |

## Outputs:

Outputs are generated in output/VISUALISE directory by default.

| Output | Description |
| :--- | :--- |
| PDB file | Output PDB to be opened in VMD |
| Arrows file | Tcl script that can be copied into the VMD TK console |

## chapter 10

## PCA Scripts

Principal component analysis (PCA) is a useful statistical technique that has found applications in detection of correlated motion in MD data. Protein dynamics is manifested as a change in molecular structure, or conformation over a timescale. PCA extracts most important motions from a protein's MD trajectory using a covariance/correlation matrix (C-matrix) constructed from atomic coordinates. Different types of coordinate systems (Cartesian or internal coordinates) can be employed to define atomic movement in each time frame of a trajectory. Modes describing the protein motions can be constructed by diagonalizing the C-matrix. It leads to a complete set of orthonormal (orthogonal and normalized) collective modes (eigenvectors) with eigenvalues (variance) that characterize the protein dynamics. The largest eigenvalues represent the most collective spatial motion. When the original mean centered data (MD trajectory) is projected on the eigenvectors, the results are called Principal Components (PC). Diagonalization of the C-matrix can be done by Eigenvalue decomposition (EVD) or Singular value decomposition (SVD), with the latter being computationally efficient.

As stated earlier, different representations of protein conformations can be used. One can choose Cartesian coordinates or internal coordinates such as the pairwise distance between atoms, 1-3 angle, torsional angles ( $\Phi$ or $\Psi$ ). Since decomposition of a C-matrix is memory intensive and very often the program will run out of memory, often a coarse graining is required such as selecting CA atoms. The user can select the subset of atoms from the trajectory for the analysis such as CA, backbone atoms or all protein's atoms. It is highly recommended that the user should strip the water from the trajectory before hand, as it would result in faster loading and alleviate the memory issues.

PCA uses linear transformation which may not be sufficient in cases where variables are non-linearly related. Thus, the user has the option to perform Nonlinear generalization of PCA such as Kernel PCA (kPCA). Caution should be given while interpreting the kPCA results since it is mapped to a feature space which is inherently different than conformational space. Nevertheless, kPCA is useful in understanding the protein's functions in terms of its conformational dynamics.

## General Usage:

To perform PCA on a protein's MD trajectory we need a sufficiently sampled MD trajectory and a corresponding topology file. This can be achieved by running the following command.

Command: pca.py -t <MD trajectory> -p <topology file>
To see the all the available options run the following command: pca.py -h
Inputs:

| Input <br> $\left({ }^{*} r e-\right.$ <br> quired $)$ | In- <br> put <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| Trajec- <br> tory file <br> $*$ | File | - t | MD trajectory input file (.xtc, .mdcrd etc.) |
| Topol- <br> ogy file <br> $*$ | File | -p | Topology file (.gro, .pdb etc) |
| Output <br> direc- <br> tory | String -out Name of the output directory. Default is out, suffixed by trajectory name |  |  |
| Atom <br> group | String - ag | Group of atoms for PCA. Default is CA atoms. Other options are: all = all atoms, <br> backbone = backbone atoms, CA = C-alpha atoms, protein = protein atoms |  |
| Refer- <br> ence <br> structure | File | -r | Reference structure for RMSD. Default: First frame of MD trajectory |
| PCA <br> method | String | -pt | PCA method. Default is svd (Single Value Decomposition) PCA. Options are: evd, kpca, <br> svd, ipca. If svd is selected, additional arguments can be passed by flag -st. If KernelPCA <br> is selected kernel type can also be defined by flag -k |
| Number <br> of com- <br> ponents | Int | - nc | Number of components to keep in a PCA object. Default: All the components will be <br> kept. |
| Kernel <br> Type | String -kt | Type of kernel for KernalPCA. Default is linear. Options are: linear, poly, rbf, sigmoid, <br> cosine, precomputed |  |
| SVD <br> solver <br> type | String -st | Type of svd_solver for SVD (Single Value Decomposition) PCA. Default is auto. Op- <br> tions are: auto, full, arpack, randomized |  |

## Outputs:

| Output | Description |
| :--- | :--- |
| PC plots | 2D Plot of first 3 PCs. It is grace formatted text file |
| PC plots (.png) | 2D Plot of first 3 PCs. Same as above, but points are color coded according to MD time |
| Scree plot | Scree plot of contribution of first 100 modes (eigenvectors) |
| RMSD plot | RMSD of selected atoms over the MD time |
| RMSD Modes | Plot of contribution of each resdiues towards the first 3 modes (eigenvectors) |

Besides the above-mentioned plots, it also prints useful information on the terminal such as, information about the trajectory, Kaiser-Meyer-Olkein (KMO) index of the trajectory, and cosine contents of the first few PCs. KMO value range from 0 to 1,1 indicating that the MD has been sampled sufficiently. The cosine content of PCA projections can be used as an indicator if a simulation is converged. Squared cosine value should be more than 0.5 .

## Specific Examples:

### 10.1 PCA on Cartesian coordinates

Given a trajectory called trajectory.xtc and a topology file called complex.pdb, the following command is used:

```
pca.py -t trajectory.xtc -p complex.pdb
```

This will perform the singular value decomposition (SVD) based PCA on CA atoms by default. To use other methods, see the following examples.

### 10.1.1 SVD PCA

To perform SVD PCA on CA atoms of a MD trajectory
Command: pca.py -t trajectory.xtc -p complex.pdb -ag CA -pt svd
To perform the SVD PCA on backbone atoms
Command: pca.py -t trajectory.xtc -p complex.pdb -ag backbone -pt svd

### 10.1.2 Kernel PCA

To perform the Kernel PCA with linear kernel
Command: pca.py -t trajectory.xtc -p complex.pdb -ag CA -pt kpca -kt linear
To perform the Kernel PCA with rbf kernel
Command: pca.py -t trajectory.xtc -p complex.pdb -ag CA -pt kpca -kt rbf

### 10.1.3 Incremental PCA

Incremental PCA (IPCA) is a variant of usual PCA, which uses low-rank approximation of the input MD trajectory. It uses the amount of memory to store the input trajectory which is independent of trajectory size. IPCA is very useful in case the size of trajectory is larger than that may be handled by the available computer memory.

Command: pca.py -t trajectory.xtc -p complex.pdb -ag CA -pt ipca

### 10.1.4 Eigenvalue decomposition (EVD) PCA

To perform the PCA by eigenvalue decomposition
Command: pca.py -t trajectory.xtc -p complex.pdb -ag CA -pt evd
Detailed usage:
Run the following command to see the detailed usage and other options: pca.py -h

### 10.2 PCA on internal coordinates

Users can also perform the PCA on internal coordinates of a MD trajectory. Options are available for different types of internal coordinates such as: pairwise distance between atoms, 1-3 angle between backbone atoms, psi angle, and phi angle.

## General Usage:

Command: internal_pca.py -t <MD trajectory> -p <topology file>

## Inputs:

| Input <br> $\left({ }^{*} r e-\right.$ <br> quired $)$ | Input <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| Trajec- <br> tory <br> $*$ | File | -t | MD trajectory input file (.xtc, .mdcrd, etc.) |
| Topology <br> file * | File | -p | Topology file (.gro, .pdb, etc) |
| Output <br> directory | String | - out | Name of the output directory. Default is out, suffixed by trajectory name |
| Atom <br> group | String | - ag | Group of atom for PCA. Default is CA atoms. Other options are: all $=$ all atoms, <br> backbone = backbone atoms, CA = C-alpha atoms, protein $=$ protein atoms |
| Coor- <br> dinate <br> Type | String | - -ct | Internal cordinate type. Options are: distance, angles, phi, and psi |

## Outputs:

| Output | Description |
| :--- | :--- |
| PC plots | 2D Plot of first 3 PCs. It is a grace formatted text file |
| PC plots (.png) | 2D Plot of first 3 PCs. Same as above, but points are color coded according to MD time |
| Scree plot | Scree plot of the contribution of the first 100 modes (eigenvectors) |

## Specific Examples:

## PCA on pairwise distance between CA atoms:

To perform the PCA on pairwise distance between CA atoms of an MD trajectory trajectory . xtc and a topology file complex.pdb

Command: internal_pca.py -t trajectory.xtc -p complex.pdb -ag CA -ct distance
PCA on psi angles:
Command: internal_pca.py -t trajectory.xtc -p complex.pdb -ct psi

## Detailed usage:

Run the following command to see the detailed usage and other options: internal_pca.py -h

### 10.3 MDS (Multi-dimensional scaling) on MD trajectory

MDS is a tool to visualize the similarity or dissimilarity in a dataset. Two types of dissimilarity measures can be used in the case of a MD trajectory. The first is Euclidean distance between internal coordinates of a protein structure, the second is pairwise RMSD between a set of atoms over the frames of a MD trajectory.

## General Usage:

command: mds.py -t <MD trajectory> -p <topology file>
Inputs:

| Input <br> $\left({ }^{*} r e-\right.$ <br> quired | In- <br> put <br> type | Flag | Description |
| :--- | :--- | :--- | :--- |
| Tra- <br> jectory <br> file $*$ | File | -t | MD trajectory input file (.xtc, .mdcrd, etc.) |
| Topol- <br> ogy file <br> * | File | -p | Topology file (.gro, .pdb, etc) |
| Output <br> direc- <br> tory | String | - out | Name of the output directory. Default is out, suffixed by trajectory name |
| Atom <br> group | String | - ag | Group of atoms for MDS. Default is CA atoms. Other options are: all $=$ all atoms, back- <br> bone $=$ backbone atoms, CA $=$ C-alpha atoms, protein $=$ protein atoms |
| MDS <br> type | String | -mt | Type of MDS. Options are nm $=$ non-metric, metric $=$ metric |
| Dis- <br> simi- <br> larity <br> type | String | - -dt | Type of dissimilarity matrix to use. euc $=$ Euclidean distance between internal coordi- <br> nates, rmsd = pairwise RMSD. Default is rmsd |
| Coor- <br> dinate <br> type | String | - ct | Internal coordinate type. Default is pairwise distance. Only used if Dissimilarity type is <br> Euclidean |
| Atom <br> indices | String | - ai | Group of atoms for pairwise distance. Default is CA atoms. Other options are: all $=$ <br> all atoms,backbone = backbone atoms, alpha = C-alpha atoms,heavy $=$ all non-hydrogen <br> atoms, minimal = CA, CB, C, N, O atoms |

## Outputs:

| Output | Description |
| :--- | :--- |
| PC plots | 2D Plot of the first 3 PCs. It is a grace formatted text file |
| PC plots (.png) | 2D Plot of the first 3 PCs. Same as above, but points are color coded according to MD time |

## Specific Examples:

## MDS on pairwise RMSD:

To perform MDS on the pairwise RMSD between CA atoms
Command: mds.py -t trajectory.xtc -p complex.pdb -dt rmsd -ag CA

## MDS on internal coordinates:

To perform MDS on the pairwise distance between CA atoms
Command: mds.py -t trajectory.xtc -p complex.pdb -dt euc -ag CA

## Detailed usage:

Run the following command to see the detailed usage and other options: mds. py -h

## 10.4 t-SNE on MD trajectory

t -distributed Stochastic Neighbor Embedding (t-SNE) is a tool for dimensionality reduction. It is a variant of stochastic neighbor embedding technique. t-SNE uses a measure of dissimilarity, which, in the case of MD trajectory, may be
the Euclidean distance between internal coordinates or pairwise RMSD.
General Usage:
Command: tsne.py -t <MD trajectory> -p <topology file>
Inputs:

| Input ( ${ }^{*}$ required) | $\begin{aligned} & \text { In- } \\ & \text { put } \\ & \text { type } \end{aligned}$ | Flag | Description |
| :---: | :---: | :---: | :---: |
| Trajectory file * | File | -t | MD trajectory input file (.xtc, .mdcrd, etc.) |
| Topology file * | File | -p | Topology file (.gro, .pdb, etc) |
| Output directory | String | -out | Name of the output directory. Default is out, suffixed by trajectory name |
| Atom group | String | -ag | Group of atoms for t-SNE. Default is CA atoms. Other options are: all = all atoms, backbone $=$ backbone atoms, $\mathrm{CA}=\mathrm{C}$-alpha atoms, protein $=$ protein atoms |
| Coordinate type | String | -ct | Internal coordinates type. Default is pairwise distance . Only used if Dissimilarity type is Euclidean |
| Dissimilarity type | String | -dt | Type of dissimilarity matrix to use. euc = Euclidean distance between internal coordinates, rmsd = pairwise RMSD. Default is rmsd |
| Atom indices | String | -ai | Group of atoms for pairwise distance. Default is CA atoms. Other options are: all = all atoms, backbone $=$ backbone atoms, alpha $=\mathrm{C}$-alpha atoms, heavy $=$ all non-hydrogen atoms, minimal $=\mathrm{CA}, \mathrm{CB}, \mathrm{C}, \mathrm{N}, \mathrm{O}$ atoms |
| PER-PLEXITY | Float | -pr | [t-SNE parameters] The perplexity is related to the number of nearest neighbors that is used in other manifold learning algorithms Default is 30 |
| LEARNING_RAT | Float E | -lr | [t-SNE parameters] The learning rate for t-SNE. Default is 200 |
| N_ITER | Int | -ni | [t-SNE parameters] Number of iteration to run. Default is 300 |

## Outputs:

| Output | Description |
| :--- | :--- |
| PC plots | 2D Plot of the first 3 PCs. It is grace formatted text file |
| PC plots (.png) | 2D Plot of the first 3 PCs. Same as above, but point are color coded according to MD time |

## Specific Example:

t-SNE on CA atoms: To perform t-SNE using the pairwise RMSD of CA atoms as index of dissimilarity.
command: tsne.py -t trajectory.xtc -p complex.pdb -ag CA -dt rmsd
To perform t-SNE using the Euclidean space between pairwise distance of CA atoms as index of dissimilarity.
command: tsne.py -t trajectory.xtc -p complex.pdb -ag CA -dt euc -ai alpha

## Detailed usage:

Run the following command to see the detailed usage and other options: tsne.py -h

## CHAPTER 11

NMA Tutorial

Enterovirus 71 (EV-71) is a human pathogen that predominantly infects small children. The capsid is icoshedral and contains 60 protomer units. In a mature capsid the protomers are assembled as a set of 12 pentamers. Each protomer contains a single copy of the proteins VP1-VP4. During infection, the virus capsid expands to release its RNA into the host cell. This expanded capsid is known as the A-particle.

### 11.1 Aim

In this tutorial we will apply the ANM model to a single pentamer of the mature EV-71 capsid. We aim to identify the normal modes that contribute to the conformational changes within a pentamer during capsid expansion.

### 11.2 Create a working directory

First create a directory for all the MODE-TASK scripts using the Linux command:

```
mkdir ModeTask
```

Copy the entire contents of the MODE-TASK Scripts into the MODE-TASK directory.
Within this directory create a folder called Tutorial:

```
cd ModeTask
```

mkdir Tutorial

We will run all scripts from the ModeTask directory.

### 11.3 Preparation of structure of the mature capsid

1) Download the 3 VBS biological assembly (3VBS.pdb1) of the mature EV-71 capsid from the PDB.
2) Open 3VBS.pdb1 in PyMOL.
3) Use the split_states 3VBS command to visualise the full capsid.
4) Save the capsid: File - Save Molecule - Select the first five states. Save as EV71_Pentamer.pdb into the ModeTask/Tutorial directory.
Each protomer has four subunits: VP1-VP4. VP4 is an internal capsid protein.

- Number of residues per protomer $=842$
- Number of residues per pentamer $=4210$

The estimated run time to perfom ANM on a complex of 4210 residues, using Mode Task is 25 hours.
For the sake of this tutorial we will use the coarseGrain.py script to construct a lower resolution pentamer.

### 11.4 Preparation of the structure of the A-particle capsid

1) Download the 4 N 43 biological assembly ( $4 \mathrm{~N} 43 . \mathrm{pdb} 1$ ) of the A-partcile EV-71 capsid from the PDB.
2) Open $4 N 43 . p d b 1$ in PyMOL.
3) Use the split_states $\mathbf{4 N} \mathbf{N 3}$ command to visualise the full capsid.
4) Save the capsid: File - Save Molecule - Select the first five states. Save as Apart_Pentamer.pdb into the ModeTask/Tutorial directory.

### 11.5 Coarse grain

The MODE-TASK package is designed to analyse both single proteins and larger macromolecules such as a virus capsid. The ANM.cpp script contructs an elastic network model on all CA or CB atoms in a given PDB file. This is ideal for smaller protein complexes. For larger protein complexes, the coarseGrained.py script can be used to construct an additional coarse grained PDB file.

1) Create a two models of the EV71 Pentamer complex with additional coarse graining set at levels 3 and 4 of selected CB atoms:
```
coarseGrain.py --pdb Tutorial/EV71_Pentamer.pdb --cg 3,4 --startingAtom 1 --
\hookrightarrowoutput EV71_CG3.pdb --outdir Tutorial --atomType CB
```


## The input paramaters include:

- pdb: This is the pdb structure that you wish to coarse grain
- cg: This specifies the levels of coarse graining. To select fewer atoms increase the level
- starting atom: This specifies the first residue to be selected in the complex
- output: The filename of the coarse grained pdb file
- outdir: The directory in which to save the coarse grained pdb file


## Output:

a) EV71_CG3.pdb and EV71_CG4.pdb : Two separate coarse grained pdb files that have the coordinates of selected CB atoms from residues that are equally distributed across the complex. As an example, EV71_CG3.pdb is shown in the figure below.
b) Command line output

```
====================================================================
Started at: 2017-12-12 11:34:36.399300
SUMMARY OF COARSE GRAINING PERFORMED AT LEVEL 3
No. atoms selected per unit: 122 from 842 original residues
No. atoms selected per macromolecule: 610 from 4210 orignal residues
SUMMARY OF COARSE GRAINING PERFORMED AT LEVEL 4
No. atoms selected per unit: 54 from 842 original residues
No. atoms selected per macromolecule: 270 from 4210 orignal residues
Completed at: 2017-12-12 11:34:36.541637
- Total time: 0:00:00
```

Note that, the same set of 122 atoms from each protomer were selected for CG3, likewise, the same set of 54 atoms from each protomer were selected for CG4 - thus the symmetry of the pentamer is retained.


Fig. 1: Left) Crystal structure of the EV71 Pentamer (3VBS). Right) EV71_CG3.pdb contains 610 CB atoms from 4210 total residues.

### 11.6 Mode decomposition

The ANM.cpp script accepts a PDB file and a cutoff distance. The script constructs the Hessian matrix connecting all CB atoms within the specific cutoff radius. The script then performs singular value decomposition to return the eigenvalues and eigenvectors of the Hessian matrix.

## Input parameters:

- pdb: path to PDB file
- cutoff: cutoff radius in A. The script will construct an elastic network model by connecting all atoms that interact within the cutoff distance $($ default $=15 \AA)$
- outdir: folder in which output is saved


## Output:

W_values.txt: A list of 3 N eigenvalues of the system. Eigenvalues are ordered from slowest to fastest.
VT_values.txt: A 3 Nx 3 N list of the eigenvectors for each mode. Eigenvectors are printed as a set of rows.
U_values.txt: A 3Nx3N list of the eigenvectors for each mode. Eigenvectors are printed as a set of columns.

1) Compile the ANM.cpp script

The ANM.cpp script requires classes of the AlgLib library. These classes can be found in the cpp/src folder in the GitHub Directory. The path to these classes must be specified in the compile command using the -I parameter:

```
g++ -I cpp/src/ ANM.cpp -o ANM
```

In this tutorial, we will perform a comparative analysis between the normal modes of the EV71_CG3.pdb and EV71_CG4.pdb
2) Run ./ANM to analyse EV71_CG4.pdb with a cutoff of $24 \AA$

```
./ANM --pdb Tutorial/EV71_CG4.pdb --outdir Tutorial --atomType CB --cutoff_
\hookrightarrow24
```

Example of the command line output:

```
Started at: 2017-08-22 11:55:33
Starting Decomposition
Completed at: 2017-08-22 11:55:47
- Total time: 0:00:13
```

3) Run ./ANM to analyse EV71_CG3.pdb
3.1) First make a sub-directory to avoid overwriting of your previous ANM output:
```
mkdir Tutorial/CG3
```

3.2)

```
./ANM --pdb Tutorial/EV71_CG3.pdb --outdir Tutorial/CG3 --atomType CB --cutoff 24
```

Example of command line output:

```
Started at: 2017-08-22 11:56:42
Starting Decomposition
Completed at: 2017-08-22 11:59:14
    Total time: 0:02:0-704
```


### 11.7 Identification of modes that contribute to the conformational change

We have performed ANM on two separate pentamer complexes. From each model, we have obtained a set of eigenvalues and eigenvectors corresponding to each normal mode:

1) EV71_CG4.pdb, total non-trivial modes $=804$
2) EV71_CG3.pdb, total non-trivial modes $=1824$

For each model we will now identify the modes that contribute to the conformational change of a pentamer during capsid expansion.

We will then compare the modes from the respective models and determine if the additional coarse graining affected the ability to capture such modes.

To determine if our modes overlap with the direction of the conformational change, we must first determine the conformational change between the crystal structures of the mature and A-particle pentamer. The conformationMode.py scripts take two UNALIGNED pdb files and the set of all eigenvectors determined for the complex. The script aligns the structures, calculates the known conformational change and then identifies which modes contribute to the change.

Prepare the A-particle pentamer in PyMOL, using the biological assembly: 4n43.pdb1

### 11.8 Conformation mode

1) Compute the overlap between all modes of the EV71_CG4 model:
```
conformationMode.py --pdbANM Tutorial/EV71_CG4.pdb --vtMatrix Tutorial/VT_
\hookrightarrowvalues.txt --pdbConf Tutorial/Apart_Pentamer.pdb --outdir Tutorial/ --
\hookrightarrowatomType CB
```


## Input paramters:

-pdbANM: This is the PDB file that you use to run ANM. Do not use the aligned file here
-vtMatrix: The eigenvalues obtained from ANM of the EV71_CG4 model
-pdbConf: This is the pdb file of the conformational change. In this case, the pentamer of the A-particle (The -pdbANM and -pdbConf must NOT BE ALIGNED)

## Output:

A text file with the overlap and correlation of each mode to the conformational change. The modes are ordered by the absolute value of their overlap.
2) Compute overlap between all modes of the EV71_CG3 model (Remember to specify the correct directory):

```
conformationMode.py --pdbANM Tutorial/EV71_CG3.pdb --vtMatrix Tutorial/CG3/
GT_values.txt --pdbConf Tutorial/Apart_Pentamer.pdb --outdir Tutorial/CG3_
\hookrightarrow--atomType CB
```

Top output from conformationalMode.py of EV71_CG4:

| MODE | Overlap | Correlation |
| :--- | :---: | :--- |
| Mode: 9 | 0.759547056636 | 0.502678274421 |
| Mode: 37 | 0.274882204134 | 0.0404194084198 |
| Mode: 36 | -0.266695656516 | 0.116161361929 |
| Mode: 23 | 0.260184892921 | 0.0752811758038 |
| Mode: 608 | 0.224274263942 | 0.0255344947974 |
| Mode: 189 | -0.208122679764 | 0.143874874887 |
| Mode: 355 | 0.165654954812 | 0.0535734675763 |
| Mode: 56 | 0.14539061536 | 0.11985698672 |
| Mode: 387 | -0.137880035134 | 0.245587436772 |
| Mode: 307 | -0.130040876389 | 0.145317107434 |

Top output from conformationalMode.py of EV71_CG3:

| MODE | Overlap | Correlation |
| :--- | :--- | :--- |
| Mode: 9 | -0.663942246191 | 0.236900852193 |
| Mode: 30 | -0.235871923574 | 0.192794743468 |
| Mode: 56 | 0.159507003696 | 0.083164362262 |
| Mode: 101 | 0.157155354273 | 0.272502734273 |
| Mode: 172 | 0.156716125374 | 0.275230637373 |
| Mode: 166 | -0.153026188385 | 0.332283689479 |
| Mode: 189 | -0.147803049356 | 0.372767489438 |
| Mode: 38 | -0.13204901279 | 0.196369524407 |
| Mode: 423 | -0.131685652034 | 0.334715006091 |
| Mode: 76 | -0.129977918229 | 0.296798866026 |

In addition, the command line output will specify the precise atoms over which the calculations were performed. (Of course, this will correspond to all atoms that are present in both conformations). The RMSD between the two structures will also be specified:

```
Started at: 2017-12-12 12:50:48.922586
********************************************************************
WARNING!!!:
Not all chains from PDB files were selected
Suggested: Chain IDs do not match between PDB Files
*******************************************************************
Correlations calculated across 465 common residues (93 per 5 asymmetric,
\hookrightarrowunits).
Breakdown per chain:
A: 32 residues per asymmetric unit
Residues selected include: 74 79 92 98 101 105 108 112 122 139 142 148 1554
\hookrightarrow158 161 171
```



```
\hookrightarrow273 282
    290293
B: 29 residues per asymmetric unit
Residues selected include: 17 37 44 58 65 76 79 83 90 108 115 128 134 141)
\hookrightarrow151 155 180
    186 189 202 208 219 222 227 231 234 241 245 249
C: 32 residues per asymmetric unit
Residues selected include: 2 7 12 12 15 18 28 32 36 40 65 78 82 86 92 98 104,
4112 133 139
    147 152 158 169 174 202 205 209 214 219 222 229,
\hookrightarrow233
*****************************************************************
RMSD between the two conformations = 3.95802072351
Completed at: 2017-12-12 12:50:49.269902
- Total time: 0:00:00
```


### 11.9 Combination mode

This option allows to calculate the overlap and correlation to a conformational change, over a combination of modes. In this example, we will use the EV71_CG3 Model and perform the calculation over the modes 9 and 30.

> combinationMode.py -pdbANM Tutorial/EV71_CG3.pdb -vtMatrix Tutorial/CG3/VT_values.txt -pdb-

Conf Tutorial/Apart_Pentamer.pdb -modes 9,30 -outdir Tutorial/CG3 -atomType CB

## Output from combinationMode.py

The command line output is the same as described for conformationMode.py
The script will also print out two text files:

1) A file that specifies that calculated overlap and correlation over the full model:

| MODE | Overlap | Correlation |
| :---: | :---: | :---: |
| Mode: 9 | -0.663942246191 | 0.236900852193 |
| Mode: 30 | -0.235871923574 | 0.192794743468 |
| ```l Combined Correlation = 0.219893695954``` |  |  |
|  |  |  |
|  |  |  |
| ********* | **************** | *************** |

2) A file that gives a breakdown of the calculated overlap and correlation per chain in each asymmetric unit of the model. This is very useful for identifying which regions of the complex contribute the most to the conformational change for a given mode:
```
======================================================================
======================================================================
ASYMMETRIC UNIT: 1
CHAIN: A
MODE Overlap Correlation
Mode: 9 -0.677454134085 0.101259205597
Mode: 30 -0.396594527376 0.601345215538
Combined Overlap = 0.620398046618
Combined Correlation = 0.337867917512
--------------------------------------------------------------------------
CHAIN: B
MODE Overlap Correlation
Mode: 9 -0.717931968623 0.491498558701
Mode:30 -0.348260895864 0.249005547277
Combined Overlap = 0.679846136775
Combined Correlation = 0.321369216974
CHAIN: C
MODE Overlap Correlation
Mode: 9 -0.637082761027 0.198091140187
Mode:30 0.0309855898365 0.149051660589
Combined Overlap = 0.532447057412
```



### 11.10 Mode visualisation

From each model we have identified which mode overlaps the most with the direction of the conformational change. We can now project these vectors onto the respective models using the visualiseVector.py script and then visualise them as a set of frames in VMD:

1) Standard visualisation This option uses the default settings: Radius of arrow head $=2.20$ Radius of arrow tail $=0.80$

Arrow are coloured by chain in ascending order of PDB file according to the list:
In a biological assembly, respective chains from each asymmetric unit are presented in the same colour. The script can handle 20 non-identical changes, after which all arrows will be coloured black by default
1.1) Visualise eigenvectors for mode 9 of the CG4 model. Note this overlap is positive, thus the vectors act in the direction to conformational change. Therefore we can specify the direction as 1 (or rely on the default setting of direction $=1$ ) when visualising the vectors:
visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -direction 1 -outdir Tutorial OR visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -outdir Tutorial
1.2) Visualise eigenvectors for mode 9 of the CG3 model. Note this overlap is negative, thus the vectors act in the opposite direction to conformational change. Therefore we must specify the direction as -1 when visualising the vectors:
visualiseVector.py -pdb Tutorial/CG3/EV71_CG3.pdb -vtMatrix Tutorial/CG3/VT_values.txt -mode 9
-atomType CB -direction -1 -outdir Tutorial/CG3

## Output from visualiseVector.py

The script will produce a folder named VISUALISE. For every mode that you give to visualiseVector.py two files will be produced:

1) A VISUAL PDB file. This can be opened in VMD and visualised as a set of 50 frames.
2) A VISUAL_ARROWS text file. This file contains a Tcl script that can be copied into the VMD TK console. The script plots a set of arrows indicating the direction of each atom.

## Visualising the results in VMD

1) Open VMD.
2) To load the VISUAL_9.pdb file click the following tabs: File >> New Molecule >> Browse >> Select VISUAL_9.pdb.
3) The VISUAL_9.pdb file contains a set of 50 frames of the eigenvectors of mode 9. This can be visualised as a movie by clicking on the Play button. The frame set can also be coloured to the user's desire using the options under the Graphics >> Representations
4) The VISUAL_ARROWS text file contains a script that can be copied and pasted straight into the Tk Console in VMD: Extensions >> Tk Console
5) To obtain a clearer observation, change the background to white: Graphics >> Colors >> Under Categories select Display >> Under Names select Background >> Under Colors select White
6) To obtain only the arrows, delete all frames of the VISUAL_9.pdb molecules: Right click on the number of frames >> Delete frames >> Delete frames 0 to 49
7) Alternatively you can plot the arrows onto the original PDB (uncoarse grained) PDB file and visualise it in cartoon format: Load EV71_Pentamer.pdb into VMD >>"Graphics >> Representations >> Drawing method >> NewCartoon" >> copy and paste the VISUAL_ARROWS text file into the Tk Console. To improve clarity under the NewCartoon options select: Material >> Transparent Spline Style >> B-Spline
8) To colour tha protein complex by chain: Graphics >> Colours >> Under Categories select Chain >> Under Name select A >> Under Colours select Red To match the arrows colours as: Chain $\mathrm{A}=$ Red Chain $\mathrm{B}=$ Blue Chain $\mathrm{C}=$ Orche Chain $\mathrm{D}=$ Purple Finally instruct VMD to colour by chain Graphics >> Representations >> Coloring Method >> Chain


Fig. 2: Fig: Visualisation in VMD. Left) Only arrows depicted Right) Arrows plotted onto cartoon depiction of pentamer
2) Additional options for visualisation

Here you have the options to: 2.1) Change the thickness and length of the arrows 2.2) Specify the colours of the arrows for each change 2.3) Visualise the motion and draw arrows for a single or specified set of asymmetric units 2.4) Draw arrows for a single chain

We will demonstrate each of the above options using the EV71_CG4 model.
2.1) Change the thickness and length of the arrows Here we will increase the thickness of the arrow head to 3.0 , increase the thickness of the arrow tail to 1.5 and the increase the length pf each arrow by a factor of 2
visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -outdir Tutorial -head 3.0-tail 1.5 -arrowLength 2
2.2) specify the colours of the arrows for each change

Here we will colour the arrows as follows: Chain $\mathrm{A}=$ Yellow Chain $\mathrm{B}=\mathrm{Blue}$ Chain $\mathrm{C}=$ Pink Chain $\mathrm{D}=$ Green visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -outdir Tutorial -colourByChain yellow,blue,pink,green
2.3) Visualise the motion and draw arrows for a single or specified set of asymmetric units

Here we will visualise the motion of asymmetric units 1 and 3 .
visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -outdir Tutorial-aUnits 1,3

The motion will be captured in the frame set: VISUAL_AUNITS_9.pdb in the Tutorial folder, and can be played in VMD.
2.4) Draw arrows for a single chain

Here we will draw arrows only for A chain of asymmetric unit 1 of the EV71_CG4 pentamer, in colour gray visualiseVector.py -pdb Tutorial/EV71_CG4.pdb -vtMatrix Tutorial/VT_values.txt -mode 9 -atomType CB -outdir Tutorial -aUnits 1 -chain A -colourByChain gray


Fig. 3: Fig: Visualisation in VMD after increasing arrow sizes


Fig. 4: Fig: Visualisation in VMD with arrows coloured as specified by user


Fig. 5: Fig: Vectors arrows for asymmetric units 1 and 3 of the pentamer


Fig. 6: Fig: Vectors arrows for Chain A of asymmetric units 1 in colour gray

### 11.11 Mean square fluctuation (MSF)

Next, we will use the meanSquareFluctuations.py script to calculate the MSF of the CB atoms. The scripts allows you to calculate:
a) the MSFs, calculated over all modes
b) the MSFs of the CB atoms for a specific mode, or a specific range of modes.

The script also allows for comparison of MSF obtained from modes of different models. We can use the -pdbConf2 parameter to send the script a second PDB model. The script will then calculate the MSF of atoms corresponding to residues that are common between both models.

In this tutorial, we will analyse and compare the MSF between EV71_CG4 and EV71_CG3. This will give an indication as to whether or not the higher coarse grained model is also suitable to study the virus.

1) We will compare the MSFs between the two models for a) all modes, and b) mode 9
```
meanSquareFluctuation.py --pdb Tutorial/EV71_CG3.pdb --wMatrix Tutorial/CG3/
W_values.txt --vtMatrix Tutorial/CG3/VT_values.txt --pdbConf2 Tutorial/
๑EV71_CG4.pdb --wMatrixC Tutorial/W_values.txt --vtMatrixC Tutorial/
\hookrightarrowVT_values.txt --modes 9 --outdir Tutorial/ --atomType CB
```


## Output for Model CG3:

1) PDB1_msf.txt: Text file of the overall MSFs values for all residues of CG3
2) PDB1__msfSpecificModes.txt: MSFs for all residues for mode 9 of CG3
3) PDB1CommonResidues_msf.txt: Overal MSFs for residues (of CG3) common to CG3 and CG4
4) PDB1_CommonResidues_msfSpecificModes.txt: MSFs for residues (of CG3) common to CG3 and CG4 calculated for mode 9
Output for Model CG4:
5) PDBCompare_msf.txt:: Text file of the overall MSFs values for all residues of CG4
6) PDBCompare__msfSpecificModes.txt: MSFs for all residues for mode 9 of CG4
7) PDBCompareCommonResidues_msf.txt: overal MSFs for residues (of CG4) common to CG4 and CG3.
8) PDBCompare_CommonResidues_msfSpecificModes.txt: MSFs for residues (of CG4) common to CG4 and CG3 calculated for mode 9

### 11.12 Assembly Covariance

Now, we will use the assemblyCovariance.py script to calculate to plot various covariance matrices of the complex. For this example we will use the EV71_CG3 Model.
a) First, we will plot the overall covariance for the full model, as calculated over all modes:
assemblyCovariance.py -pdb Tutorial/EV71_CG3.pdb -wMatrix Tutorial/CG3/W_values.txt -vtMatrix Tutorial/CG3/VT_values.txt -modes all -outdir Tutorial/CG3/ -atomType CB
The above function will produce a plot corresponding to the full model, AND as a default a second plot that zooms into the first asymmetric unit will also be produced
b) Now we will use the additional options to calculate the covariance for mode 7 only (the first non-trivial mode). We will also plot the covariance between the asymmetric units 1 and 3, and then zoom into chain A of the first asymmetric unit. We have also adjusted the values of the axes to increase sensitivity for a single mode.
assemblyCovariance.py -pdb Tutorial/EV71_CG3.pdb -wMatrix Tutorial/CG3/W_values.txt -vtMatrix Tutorial/CG3/VT_values.txt -modes 7 -aUnits 1,3-zoom 1,A -outdir Tutorial/CG3/M7 -atomType CB -vmin - 0.005 -vmax 0.005

The above function will produce a plot corresponding to the full model for mode 7, a second plot that zooms into covariance between the first and third asymmetric units, and a third plot for the covariance of Chain A and Unit 1.

For each of the steps above, the script also outputs each covariance matrix in txt file format.



Fig. 7: Fig: Overall covariance matrix for the full EV71_CG3 Model


Fig. 8: Fig: Overall covariance matrix for a single protomer within the EV71_CG3 Model


Fig. 9: Fig: Covariance matrix for the full EV71_CG3 Model calculated over Mode 7


Fig. 10: Fig: Covariance matrix for the asymmetric units 1 and 3 of the EV71_CG3 Model calculated over Mode 7


Fig. 11: Fig: Covariance matrix for Chain A in asymmetric units 1 the EV71_CG3 Model calculated over Mode 7

## CHAPTER 12

## PCA Tutorial

### 12.1 PCA of a MD trajectory

In this tutorial, we will be performing PCA on a MD trajectory of protein. Before doing the PCA, we need to prepare the trajectory which includes removing periodicity and removing water molecules. Most of the MD packages have options to do this. We will be using GROMACS in this tutorial. We will be using .xtc format for trajectory and .pdb for topology file. Any other common trajectory format should also work with MODE-TASK.

## 1. Preparation of trajectory

### 1.1. Remove periodicity

```
gmx_mpi trjconv -s md_01.tpr -f md_01.xtc -o md_01_noPBC.xtc -pbc mol -ur_
compact
```

select system to apply it.

### 1.2. Remove water

```
gmx_mpi trjconv -s md_01.tpr -f md_01_noPBC.xtc -o md_01_noWAT.xtc -n index
```

and select protein

## 2. Create a working directory

First, create a directory for all the MODE-TASK scripts using the Linux command:

```
mkdir ModeTask
```

Copy the entire contents of the MODE-TASK scripts into the MODE-TASK directory.
Within this directory create a folder called Tutorial:

```
cd ModeTask
mkdir Tutorial
```

We will run all scripts from the MODE-TASK directory. Move the trajectory (md_01_noWAT.xtc) and topology file (complex.pdb) into the Tutorial directory.

## 3. Running PCA

MODE-TASK includes tools to perform PCA on Cartesian coordinates as well as internal coordinates. It also allows users to run different variants of PCA on a single MD trajectory.

### 3.1. PCA on Cartesian coordinates

Run the following command to perform the singular value decomposition (SVD) PCA on CA atoms.

```
pca.py -t Tutorial/md_01_noWAT.xtc -p Tutorial/complex.pdb -ag CA -pt svd
```


## Output:

(a)- Various output files are written to the out_md_01_noWAT.xtc directory. 2D Plot of first 3 PCs, Scree plot, RMSD plot, and RMSD Modes plot. For details about these output files, please refer to the MODE-TASK documentation.
(b)- Command line output: Following output is redirected to command line.

```
Results will be written in out_md_01_noWAT.xtc
Reading trajectory Tutorial/md_01_noWAT.xtc ...
No reference structure given, RMSD will be computed to the first frame in
\hookrightarrowthe trajectory
Trajectory info:
Total }101\mathrm{ frames read from Tutorial/md_01_noWAT.xtc
MD time is from 199000.0 to 200000.0 ps
1 3 2 4 4 \text { atoms and 861 residues in the trajectory}
Atom group selected for PCA: CA
Total 860 CA atoms selected for analysis
KMO for input trajectory is 5.25051335835e-06
RMSD written to rmsd.agr
Performing SVD (Single Value Decomposition) PCA with 'auto' svd_solver
Trace of the covariance matrix is: 4.9427056479
cosine content of first PC= 0.777934456531
cosine content of second PC= 0.643848137376
cosine content of 3rd PC= 0.70061477062
cosine content of 4th PC= 0.530112237076
```


### 3.2. Visualizing the results

2D Plot of the first 3 PCs in grace and png format is written. In order to open the .agr file with xmgrace run the following command.

```
xmgrace out_pca_test_trj.xtc/pca_projection1_2.agr
```

You can also visualize the .png format figure plot by opening it with your favorite picture visualizer. In the same way, open the rmsd.agr and pca_variance.agr.

### 3.3. PCA on internal coordinates

One can also do PCA on internal coordinates of a MD trajectory. Options are available for different types of internal coordinates such as, pairwise distance between atoms, 1-3 angle between backbone atoms, phi angle, and psi angle. Run the following command to do PCA on pairwise distance between CA atoms.

```
internal_pca.py -t Tutorial/md_01_noWAT.xtc -p Tutorial/complex.pdb -ag CA -
ct distance
```

Run the following command to do PCA on backbone psi angles.


Fig. 1: plot of PC1 and PC2


Fig. 2: plot of PC1 and PC3

## explained_variance of PCs



Fig. 3: Explained variance of PCs

```
internal_pca.py -t Tutorial/md_01_noWAT.xtc -p Tutorial/complex.pdb -ag CA -
ct psi
```

Output files include 2D plot of first 3 PCs and Scree plot, which can be visualized using xmgrace as described earlier.

### 12.2 MDS (Multi-dimensional scaling) on a MD trajectory

To perform the MDS on pairwise RMSD between C-alpha atoms, run the following command.

```
mds.py -t Tutorial/md_01_noWAT.xtc -p Tutorial/complex.pdb -ag CA -dt rmsd
```

Output files include 2D plot of first three PCs which can be visualized using xmgrace as described earlier.


Fig. 4: plot of PC1 and PC2

## 12.3 t-SNE on a MD trajectory

Run the following command to perform t-SNE using pairwise RMSD of CA atoms as the index of dissimilarity.


Fig. 5: plot of PC 1 and PC 3

```
tsne.py -t Tutorial/md_01_noWAT.xtc -p Tutorial/complex.pdb -ag CA -dt rmsd
```

Output files include 2D plot of the first 3 PCs, which can be visualize using xmgrace as described earlier.
Note: The t-SNE algorithm is non-linear and highly flexible, which makes it difficult to interpret the results. Different set of parameters gives very different output. Users are required to try different set of values for "perplexity", "learning rates", and "number of iteration". A useful discussion covering these issues can be found here https://distill.pub/2016/ misread-tsne/


Fig. 6: plot of PC1 and PC2


Fig. 7: plot of PC1 and PC3

# chapter 13 

## pyMODE-TASK- PyMOL plugin

Kindly see the pyMODE-TASK documentaion for further details.


[^0]:    ${ }^{1}$ C Atilgan, OB Okan, AR Atilgan, "Network-based Models as Tools Hinting at Non-evident Protein Functionality," Annual Review of Biophysics, 41, 205-225 (2012).
    ${ }^{2}$ AR Atilgan, SR Durell, RL Jernigan, MC Demirel, O Keskin, I Bahar, "Anisotropy of Fluctuation Dynamics of Proteins with an Elastic Network Model," Biophysical Journal, 80, 505-515.

[^1]:    ${ }^{3}$ C Atilgan, OB Okan, AR Atilgan, "Orientational Order Governs Collectivity of Folded Proteins," Proteins: Structure, Function, Bioinformatics, 78, 3363-3375 (2010).

[^2]:    ${ }^{4}$ A Amadei, ABM Linssen, HJC Berendsen, "Essential Dynamics of Proteins," Proteins: Structure, Function and Genetics, 17, 412-425 (1993).

[^3]:    ${ }^{5}$ CC David, DJ Jacobs, "Principal component analysis: a method for determining the essential dynamics of proteins," Methods in Molecular Biology, 1084, 193-226 (2014).

[^4]:    ${ }^{6}$ Pedregosa F, Varoquaux G, Gramfort A, Michel V, Thirion B, Grisel O, et al. Scikit-learn: Machine Learning in Python. J. Mach. Learn. Res. 2011;12:2825-30.
    ${ }^{7}$ Ross DA, Lim J, Lin R-S, Yang M-H. Incremental Learning for Robust Visual Tracking. Int. J. Comput. Vis. 2008;77:125-41.

[^5]:    ${ }^{8}$ Van der Maaten L, Hinton G. Visualizing Data using t-SNE. J. Mach. Learn. Res. 2008;9:2579-605.

